

**Example 33: Verifying displacements of a plate with a hole**

**1 Description of the problem**

To verify the mathematical model of *ELPLA* for computing plane stresses, results of a plate with a hole introduced by *Thakkar* (2017) are compared with those obtained by *ELPLA*. A rectangular plate of dimensions 1000 [mm] × 600 [mm] and thickness 1 [mm], has a central circular hole of a diameter 200 [mm] as shown in Figure 92. The plate is subjected to a tensile stress  $\sigma_o = 500$  [N/mm<sup>2</sup>] its sides.

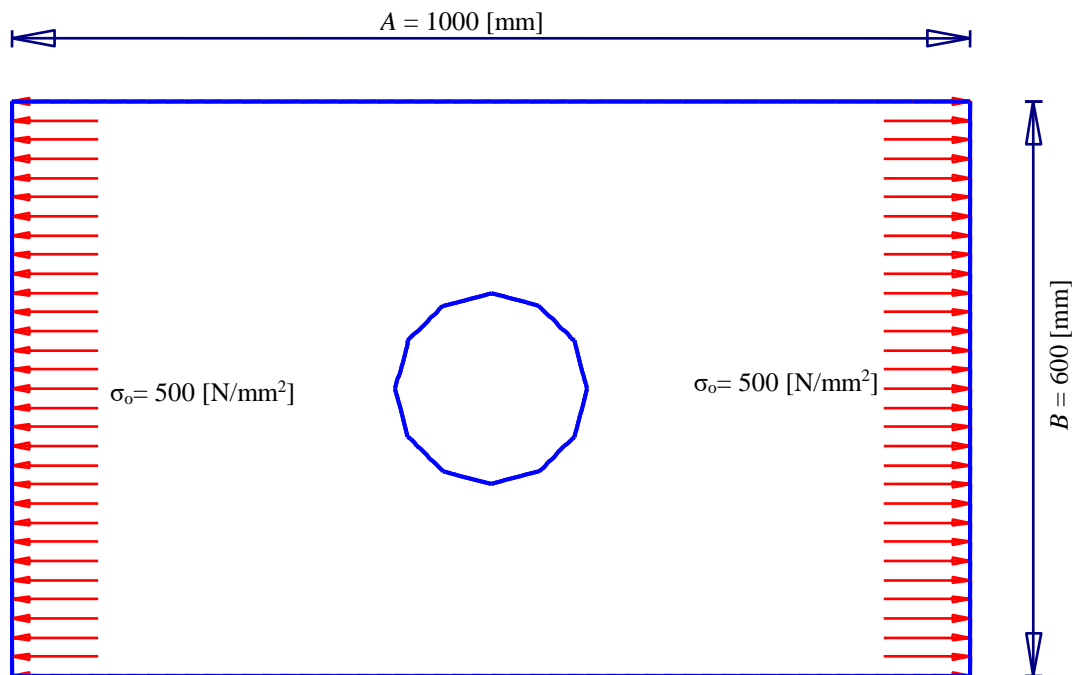


Figure 92 Plate with a hole

**2 Plate dimensions**

The plate has the following dimensions:

Plate length	$A = 1000$	[mm]
Plate width	$B = 600$	[mm]
Plate thickness	$t = 1$	[mm]

**3 Plate material**

Material of the plate has the following parameters:

Young's modulus	$E_b$	$= 2 \times 10^5$	[N/mm <sup>2</sup> ]
Poisson's ratio	$\nu_b$	$= 0.3$	[-]
Unit weight	$\gamma_b$	$= 0$	[N/mm <sup>3</sup> ]

The self-weight of the plate is ignored.

Examples to verify and illustrate *ELPLA*

#### 4 Analysis

Figure 93 shows the finite element mesh of the plate, which consists of 5700 elements. Boundary conditions are used by *Thakkar* (2017) to ensure the symmetry conditions as shown in the figure. Tensile stress  $\sigma_o = 500$  [N/mm<sup>2</sup>] on the sides are replaced by point forces on side nodes, each of 10000 [N].

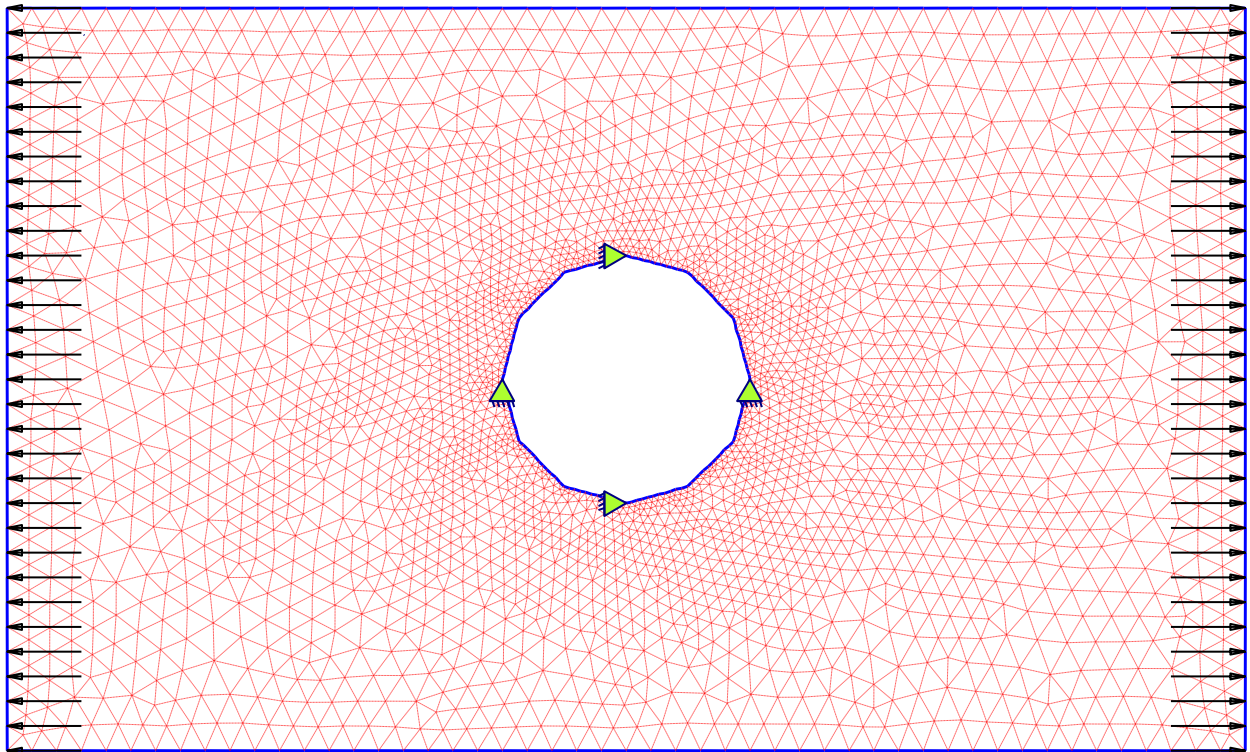


Figure 93 Finite element mesh with loads and boundary conditions

#### 5 Results

Results of *ELPLA* are compared with the that of *Thakkar* (2017) in Table 48. From this table, it can be noticed that results of maximum and minimum displacements obtained by *ELPLA* are the same as those of *Thakkar* (2017).

Table 48 Comparison of displacements obtained by *ELPLA* and *Thakkar* (2017)

Case	Displacements obtained by <i>Thakkar</i> (2017)		Displacements obtained by <i>ELPLA</i>	
	$u$ [mm]	$v$ [mm]	$u$ [mm]	$v$ [mm]
Max.	1.597	0.488	1.597	0.488
Min.	-1.597	-0.488	-1.597	-0.488